

Computer Science 120  
Course Outline

1. Any questions, comments, etc.?  
2. Discuss any difficulties or questions about last test.  
3. Review grading procedure and W policy  
4. MAT Functions --
1. DIM statement (determines space limit; includes zeroth element or row zero and column zero which are NOT used by MAT functions.)

5. MAT READ

10 DIM D(10,20) !limit of  $11 \times 21 = 231$  elements  
20 MAT READ D !reads from DATA into the array, row by row

MAT READ D(7,12) would change the size and shape of D but not the maximum number of elements ---one subscript might even exceed the original limits.

6. MAT PRINT

punctuation: none, comma, semicolon  
100 MAT PRINT 5;

7. MAT INPUT

200 MAT INPUT AS !note the possibility of a string matrix

8. ZER, CON, IDN

100 MAT A = CON !sets elements of A each equal to one  
120 MAT B = ZER(5) !to redimension B and zero the array  
130 MAT C = IDN ! sets elements on principal diagonal to 1, others to 0  
! these are the elements for which the row & column index  
! are equal to each other

9. Arithmetic with Matrices

100 MAT A = 100 !

110 MAT B = 200 !

120 MAT C = A + B !

130 MAT D = A - B !

140 MAT E = A \* B !

150 MAT F = A / B !

160 MAT G = A \ B !

170 MAT H = A . B !

180 MAT I = A .\ B !

190 MAT J = A ^ B !

200 MAT K = B ^ A !

210 MAT L = A ^ 2 !

220 MAT M = A ^ -1 !

230 MAT N = A ^ 1/2 !

240 MAT O = A ^ 3/2 !

250 MAT P = A ^ 1/3 !

260 MAT Q = A ^ -1/2 !

270 MAT R = A ^ -3/2 !

280 MAT S = A ^ 1/6 !

290 MAT T = A ^ -1/6 !

300 MAT U = A ^ 1/4 !

310 MAT V = A ^ -1/4 !

320 MAT W = A ^ 1/8 !

330 MAT X = A ^ -1/8 !

340 MAT Y = A ^ 1/16 !

350 MAT Z = A ^ -1/16 !

1010 MAT A = B + C !

1020 MAT B = A - C !

1030 MAT C = A \* B !

1040 MAT D = A / B !

1050 MAT E = A \ B !

1060 MAT F = A . B !

1070 MAT G = A .\ B !

1080 MAT H = A ^ B !

1090 MAT I = B ^ A !

1100 MAT J = A ^ 2 !

1110 MAT K = A ^ -1 !

1120 MAT L = A ^ 1/2 !

1130 MAT M = A ^ -1/2 !

1140 MAT N = A ^ 1/3 !

1150 MAT O = A ^ -1/3 !

1160 MAT P = A ^ 1/6 !

1170 MAT Q = A ^ -1/6 !

1180 MAT R = A ^ 1/8 !

1190 MAT S = A ^ -1/8 !

1200 MAT T = A ^ 1/16 !

1210 MAT U = A ^ -1/16 !

1220 MAT V = A ^ 1/32 !

1230 MAT W = A ^ -1/32 !

1240 MAT X = A ^ 1/64 !

1250 MAT Y = A ^ -1/64 !

1260 MAT Z = A ^ 1/128 !

1270 MAT A = B + C !

1280 MAT B = A - C !

1290 MAT C = A \* B !

1300 MAT D = A / B !

1310 MAT E = A \ B !

1320 MAT F = A . B !

1330 MAT G = A .\ B !

1340 MAT H = A ^ B !

1350 MAT I = B ^ A !

1360 MAT J = A ^ 2 !

1370 MAT K = A ^ -1 !

1380 MAT L = A ^ 1/2 !

1390 MAT M = A ^ -1/2 !

1400 MAT N = A ^ 1/3 !

1410 MAT O = A ^ -1/3 !

1420 MAT P = A ^ 1/6 !

1430 MAT Q = A ^ -1/6 !

1440 MAT R = A ^ 1/8 !

1450 MAT S = A ^ -1/8 !

1460 MAT T = A ^ 1/16 !

1470 MAT U = A ^ -1/16 !

1480 MAT V = A ^ 1/32 !

1490 MAT W = A ^ -1/32 !

1500 MAT X = A ^ 1/64 !

1510 MAT Y = A ^ -1/64 !

1520 MAT Z = A ^ 1/128 !

1530 MAT A = B + C !

1540 MAT B = A - C !

1550 MAT C = A \* B !

1560 MAT D = A / B !

1570 MAT E = A \ B !

1580 MAT F = A . B !

1590 MAT G = A .\ B !

1600 MAT H = A ^ B !

1610 MAT I = B ^ A !

1620 MAT J = A ^ 2 !

1630 MAT K = A ^ -1 !

1640 MAT L = A ^ 1/2 !

1650 MAT M = A ^ -1/2 !

1660 MAT N = A ^ 1/3 !

1670 MAT O = A ^ -1/3 !

1680 MAT P = A ^ 1/6 !

1690 MAT Q = A ^ -1/6 !

1700 MAT R = A ^ 1/8 !

1710 MAT S = A ^ -1/8 !

1720 MAT T = A ^ 1/16 !

1730 MAT U = A ^ -1/16 !

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1900 MAT L = A ^ 1/2 !

1910 MAT M = A ^ -1/2 !

1920 MAT N = A ^ 1/3 !

1930 MAT O = A ^ -1/3 !

1940 MAT P = A ^ 1/6 !

1950 MAT Q = A ^ -1/6 !

1960 MAT R = A ^ 1/8 !

1970 MAT S = A ^ -1/8 !

1980 MAT T = A ^ 1/16 !

1990 MAT U = A ^ -1/16 !

2000 MAT V = A ^ 1/32 !

2010 MAT W = A ^ -1/32 !

2020 MAT X = A ^ 1/64 !

2030 MAT Y = A ^ -1/64 !

2040 MAT Z = A ^ 1/128 !

2050 MAT A = B + C !

2060 MAT B = A - C !

2070 MAT C = A \* B !

2080 MAT D = A / B !

2090 MAT E = A \ B !

2100 MAT F = A . B !

2110 MAT G = A .\ B !

2120 MAT H = A ^ B !

2130 MAT I = B ^ A !

2140 MAT J = A ^ 2 !

2150 MAT K = A ^ -1 !

2160 MAT L = A ^ 1/2 !

2170 MAT M = A ^ -1/2 !

2180 MAT N = A ^ 1/3 !

2190 MAT O = A ^ -1/3 !

2200 MAT P = A ^ 1/6 !

2210 MAT Q = A ^ -1/6 !

2220 MAT R = A ^ 1/8 !

2230 MAT S = A ^ -1/8 !

2240 MAT T = A ^ 1/16 !

2250 MAT U = A ^ -1/16 !

Day # 1. (cont)

V. System accounts and record keeping

A. PPN and password security; usage category added at Wofford

B. Usage records and the \$MONEY program

1. connect time in minutes

2. CPU time in tenths of seconds

3. device time --usually plotter

4. disk storage blocks (1 block = 512 characters)

5. Disk storage limit (quota) <sup>from</sup>

6. \$MONEY ~~adds~~ uses this information ~~from~~ disk --not inclusive of current session at terminal.

7. Kilocore tics (tenths of seconds of CPU time x % of core used)

C. System date and time functions/

1. TIME(N) -- returns a number

a. N = 0 for seconds since midnight

b. N = 1 for CPU time of current session (tenths of seconds)

c. N = 2 for connect time of current session (in minutes)

d. N = 3 for kilo-core tics for the current session (or job)

e. N = 4 for device time in minutes for the current session (or job)

2. TIME\$(N) -- returns a string

a. N=0 to return the current system time in a form like 11:57 PM  
b. N non-zero to return the time string corresponding to N minutes before midnight

3. DATE\$(N) -- returns a string

a. N = 0 for the current system date

b. N non-zero returns a date string as follows.

the last three digits of the integer N tell the number of the day in the year

the remaining digits (0,1, or 2 numbers) tell how many years since 1970.

example: DATE\$(9074) = 15-Mar-79

(note the lower case characters)

"Another  
(kind of)  
Usage I want  
to talk about."

## Computer Science 120

Day #2.

### I. Program Efficiency Hints

A. to save storage space in core

1. Combine statements on a line to save statement header space  
(Statement headers are 6 words long)

Certain statements require headers anyway

DATA, DEF, DIM, FNEND, FOR, NEXT, and REM  
use ! within statements lines for your comments and save the overhead

B. reduce the requirements for constant storage by requiring that each value be stored only once.

Consider the progressive improvements in program code:

10 AZ = 278%

20 BX = 278%

vs. 10 AZ = 288% : BX = 278%

vs. 10! AZ = 278% : BX = AZ

vs. 10 AZ,BX = 278%

C. reduce the need for subscripted addressing (this also saves time)

10 For i% = 1% to NZ

: T = X(i%)

: S = S + T

: S2 = S2 + T\*T

20 NEXT i%

D. eliminate unnecessary variables

10 A = B+C : D = A+E : F = D + G

becomes

10 F = B+C + E + G

if the intermediate values A and D are not needed elsewhere

E. use integer variables whenever possible (use % sign)  
as subscripts, many FOR ... NEXT loops, etc.

F. Use variables with the same first character as much as you can  
don't introduce a new first character unnecessarily

G. Re-use variables when you can. Make them do double duty ---but you  
pay the penalty of making it more probable that you will make  
errors in your program logic.

xxd.

B. to save computer time; writing faster code

1. use subroutines instead of user-defined functions

2. implied loops are faster than FOR ... NEXT loops (saves space also)

3. multiple IF statements might be replaced by compound IF statements  
or by ON .... GO TO .... statements

80 ON INSTR(1%, "XKBY", A\$) GO TO 100, 200, 300, 400

will go to 300 if A\$ is B

Day #2. (cont)

II. Ideas for homework.

- A. Write a user-defined function which is the inverse of DATE\$() -- i.e. which will give the date for any integer from 1 to 29365. Test your results by

FND(DATE\$(NZ)) = NZ ???

A more ambitious project is to make one which will work from 1 to 32365. Note how DATE\$ works for years after 1999.

- B. Compare multiplication with exponentiation -- which is faster???

X+N or X\*X\*X\*X.....\*X

or N = @? for N = 3? FOR N = 6,7,8 etc. Is there a crossover point f# at which it is better to change your code??

- C. Write a program which is the inverse of the TIME\$() function.

- D. Write a program to find the number of minutes and seconds since the beginning of the year.

## Day 13. Information Storage Formats.

## I. Binary number system

- a. used to represent functions of the computer
- b. 2<sup>n</sup> different symbols can be represented with n binary digits
- c. one binary digit = 1 bit of information

## II. Bytes (8 bits)

- a. 2<sup>8</sup> = 256 different things to be represented with one byte.
- b. ASCII character code, opposite to EBCDIC
  - allows for 256 different characters (alphanumeric)
- c. each character of a string is stored as one byte
  - Example: the character 'a' is 97<sub>10</sub> or 0110001 in the ASCII code

## III. Integers

- a. In the 16-bit, 2 bytes or 16-bits wide one computer word.
- b. Integers are stored in two ways on most systems
  - 1. the sign bit is placed first (most significant)
  - 2. the 15 bits to the "magnitude" + 0-bit = sign + magnitude
  - 3. Bits 0-31 contain the value of the integer in binary notation
  - 4. There are others

$2^{16} = 65,536$  values (the number from 0 to 65,535)

## IV. Complement form for negative numbers. (Two's complement)

-45 is stored as the two's complement,  $0011100101010101$

$$-45 = 1111100101010101 + 1 = 1111100101010100$$

- b. smallest integer is -32768.
- c. if 0 is not needed, an 1111111111111111 is used as -32768

• largest integer = smallest integer

$$\begin{array}{r} 1111111111111111 \\ \hline 1000000000000000 \end{array}$$

also 32767 + 1 = -32767       $1111111111111111$

## V. The word storage of floating point numbers.

## 1. IEEE word

- a. has 32 bits with the "sign bit" as before
- b. bits 31-23 convert the binary exponent to excess 128 notation
- c. bits 0-8 contain the high order four significant digits of the mantissa in normalized IEEE form

## 2. decimal word

- a. IEEE-32 converts the low order digits of the mantissa
- b. approximately 9 bits of precision:  $2^{32} = 4,294,967,296$  in 7<sup>th</sup> decimal digits
- c. the power of 2 can be from -128 to 128

$$\begin{array}{r} 10000000000000000000000000000000 \\ \hline 10000000000000000000000000000000 \end{array}$$

Day 63. (cont)

## 5. sample storage for floating point numbers

$$1385_{10} = \overset{101}{1010011102} = .1010100111 \cdot 2^{11}$$

since 1385 is positive, the sign bit is 0  
 add 128 to the exponent:  $139_{10} = 10001011_2$  (exponent bits)

omitting the first bit after the binary point, insert the  
 mantissa of the number ('hidden bit')

word 1: 0100010110101001 (or as 2 bytes) 01000101 10101001

word 2: 1100000000000000 (or as 8 bytes) 11000000 00000000

## V. Computer numbers

1. limited precision

2. not a continuous set ---and the gaps are of different sizes in  
 different parts of the number system.

as seen above, there is no number between 0 and about 1.4 E-39

## VI. functions which convert the storage format from one to another

1.  $YX = \text{ASCII}(A\$)$  returns the decimal value of the first character in A\$,  
 using the ASCII code

2.  $Y\$ = \text{CHR}(X)$  returns the string character represented by the value  
 of X, using the ASCII code

3.  $\text{CVTZ\$}$ ,  $\text{CVTF\$}$ ,  $\text{CVTZ\$}$ ,  $\text{CVTF\$}$

NB: each of these functions swaps the order of the bytes  
 the F functions swap the word order also so that a number  
 in floating point format in bytes 1,2,3,4 is converted to a  
 string with the bytes in 4,3,2,1 order.

4.  $\text{CVTZ\$(A\$,NZ)}$  ---see table in BEC manual for significance of  
 various values of NZ. Values may be added for combined effects.

5.  $Y\$ = \text{NUM\$(A)}$  produces the string that would be printed by PRINT A

6.  $Y = \text{VAL}(A\$)$  if A\$ contains the characters that form a valid number.

7.  $YZ = \text{SWAP\$(NZ)}$  interchanges the two bytes of NZ, giving new integer YZ

8.  $\text{CHANGE A\$ to X\$}$  where X\$ is a list and will contain the ASCII values  
 of the characters of A\$. X\$(0) is the length of A\$.

9.  $\text{CHANGE X\$ to A\$}$

10.  $\text{STRING(L\$,C\$)}$  creates a string of L\$ characters long where each  
 is the character represented by C\$ in ASCII code.

VII. Write a program to determine and print each bit of the representation  
 of the floating point number 678.456.

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Day #4. Logic

I. Integer variables as logical variables

- A. truth values : T = -1%; F = 0%; any non-zero value will be True  
B. Program switches ---set somewhere in program and test later

AZ = (p\$ = "stop")  
BZ = (X > 12)  
CZ = DZ and 4%  
IF AZ and (BX OR CZ) then 1280

II. bit manipulation ---using less than full word for data storage

See truth  
tables in  
DEC manual

AZ = 0110 (data word) of course there are 16 bits in our  
BZ = 1010 (mask word) computer word ---I shortened these for simplicity

function	result	comment
AZ AND BZ	0010	logical product. copy selected bits of data word & set others to 0. can be used to copy part of a word, to see if certain bits are set or set certain bits to 0.
AZ OR BZ	1110	to set selected bits to 1 and copy all others. logical sum.
AZ XOR BZ	1100	logical difference ---shows, bit by bit, where A and B differ.
AZ EQV BZ	0011	shows, bit by bit, where A and B match
AZ IMP BZ	1010	the order of AND A and B matters here sets all bits of A C except here A has a 1 and B has a 0.

Examples:

- If (AZ AND NOT 7%) = 0 same as IF AZ < 7% ??  
IF (NOT AZ and 7%) = 0 if last three bits of A are 1s  
CZ = AZ AND 240% copy bits 4-7 of A into C; perhaps this  
CZ = AZ or 12% part of the word represents data we want.  
sets bits 2 & 3 to 1s, copies all others  
CX = AZ or not 12% copies bits 2&3 and sets all others to ones.

needed operations:

1. copy word segment
2. set certain bits to 1 without changing others
3. set certain bits to 0 without changing others
4. test bit N
5. set bit N
6. turn off bit N

CZ = AZ and 240%  
AZ = AZ or 12%  
AZ = AZ AND NOT 12%  $\uparrow N \uparrow N$   
IF (AZ and 2%  $\uparrow N$ ) = 3 then (or test for 0)  
AZ = AZ and 2%  $\uparrow N$   
AZ = AZ and NOT 2%  $\uparrow N$

Day #5. Random numbers.

I. Pseudo-random number generation (one way)

A.  $R_n = C \cdot R_{n-1} \pmod{N}$

$$\begin{array}{l} N=5 \\ C=2 \\ R_0=1 \end{array} \quad \begin{array}{l} 1, 2, 4, 3, 1, 2, 4, 3, \dots \\ \text{choose large } N \text{ (32769)} \end{array}$$

B. concept of repetition length

1. define

2. depends on choice of  $N$ ,  $C$  and  $R_0$

- repetition length increases with  $N$ , so choose  $N = 2^{b-1}$  (32768)
- choose  $S$  of the form  $8n \pm 3$  where  $n$  is any positive integer

c. choose  $R_0$  to be an odd integer

- d. choose  $C$  near the square root of  $N$  for better statistical properties, although not increased repetition length.

C. divide  $R_n$  by  $N$  to get a number in the range 0 to 1

II. E. Statistical tests on random numbers (and random digits)

A. mean test -- should be near 0.5 in the above case

B. Frequency distribution test -- equal intervals should contain equal counts of randomly generated values.

C. frequency of runs test. A run of length  $k$  is a series of  $k$  consecutive numbers which is monotonic (either increasing or decreasing)

$$\text{there should be } \frac{2}{(k+1)!} [N(k^2+3k+1) - (k^3+3k^2-k-4)]$$

runs of length  $k$  in a series of  $N$  random numbers

D. runs above and below the mean test

---look for sequences which are either all above or all below the mean.  
there should be

$$\frac{1}{(k+1)!} [N(k^3+3k+1) - (k^3+3k^2-k-4)] \frac{(N-k+3)}{2^{k+1}}$$

such runs of length  $k$  in  $N$  numbers.

E. gap test few random digits

each digit should recur, in one sequence, every 10 times (on the average)  
i.e. the average "gap" between repetitions of a digit should be 10.  
This should be true for each of the digits

$$\text{Variance} = \sum_{i=1}^N (g_i - \bar{g})^2$$

VARIANCE = average value of the squared deviations from the mean.

$g_i$  = current gap

$N$  For random digits, the VARIANCE of the gaps (as above) should be 90.

$\bar{g}$  = expected mean

The maximum test

In a set of three random digits, the center one will exceed the other two in 285 out of 1000 cases.

gap = 3 (123)

III. E. Uses of Random numbers.

1. Simulation

representing portions of a non-deterministic process or of one in which the deterministic rules are unknown or difficult to apply

2. Monte Carlo techniques applied to definite integrals  
area, volume, center of mass, etc.

Possible program assignments:

- Write your own pseudo-random number generator and select poor values (then good values) of  $R_0$ ,  $C$  and  $N$  and find the repetition length in each of several cases.

✓ & see back

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2. Write a program to apply the MAXIMUM test to the random number generator used by the BASIC-PLUS RND function.
3. Write a program to find what volume is left when a sphere of radius 2 has a hole of radius 1 drilled thru it along a diameter. Use the Monte Carlo technique.
4. Write a program to find the mass of a sphere of radius  $R_0 = 2$  and density  $1 + e^{-R/R_0}$
5. Consider a set of 1000 radioactive nuclei. Each has a .02 probability of decay in one unit of time. How many decay in each of the first 20 units of time and how many remain at each step? Give each undecayed nucleus a chance to decay in each new time interval.

Day #6. Sorting

I. define problem, note importance

II. references, etc.

A. 'HEPSRT

B. 'KNUTH --The Art of Computer Programming

C. Creative Computing, vol #2 issue #6

III. bubble sort

```
500 FOR I = 1 TO N
510   FOR J = I+1 TO N
520     IF D(I) < = D(J) THEN 560
530     T = D(J)
540     D(J) = D(I)
550     D(I) = T
560   NEXT J
570 NEXT I
```

program segment to sort a list D of N items into increasing order.

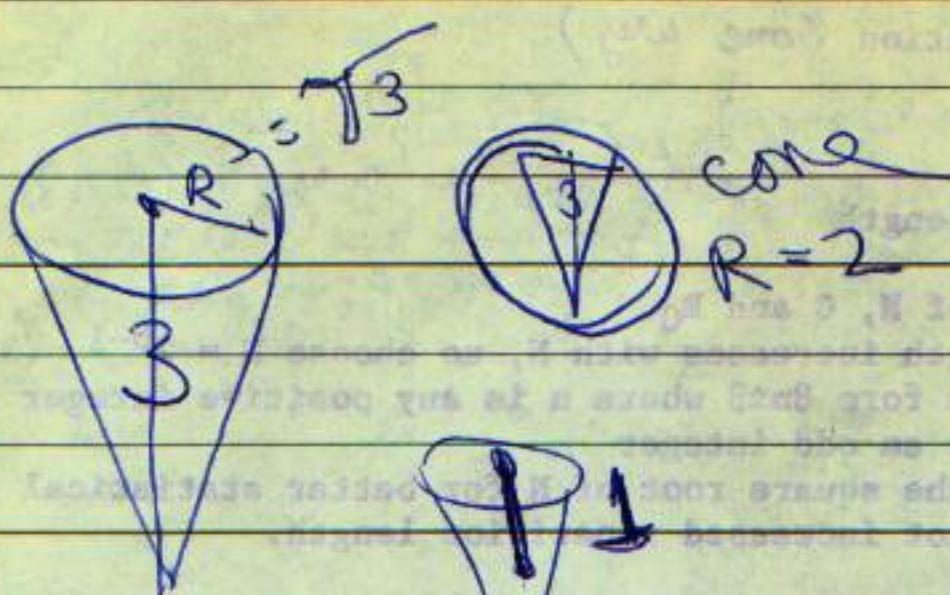
IV. delayed replacement sort

```
500 FOR K = 1 TO N
510   I = K
520   FOR J = I+1 TO N
530     IF D(I) < = D(J) THEN I = J
540   NEXT J
550   IF K = I THEN 600
560   T = D(I)
570   D(I) = D(K)
580   D(K) = T
590 NEXT K
```

V. Shell-Metzner sort/ (Shell sort modified by Marlene Metzner)

500	DATA	S	1000	DEC	1000,1000	AS1
510	INPUT	S1	100,100	I	100000	CS1
520	DATA	S2	100,100	DEC	100000	CS2
530	DATA	S3	1000,1000	I	100000	AS2
540	INPUT	S4	1000,1000	DEC	100000	CS3
550	INPUT	S5	1000,1000	DEC	100000	CS4
560	INPUT	S6	1000,1000	DEC	100000	CS5
570	INPUT	S7	1000,1000	DEC	100000	CS6
580	INPUT	S8	1000,1000	DEC	100000	CS7
590	INPUT	S9	1000,1000	DEC	100000	CS8

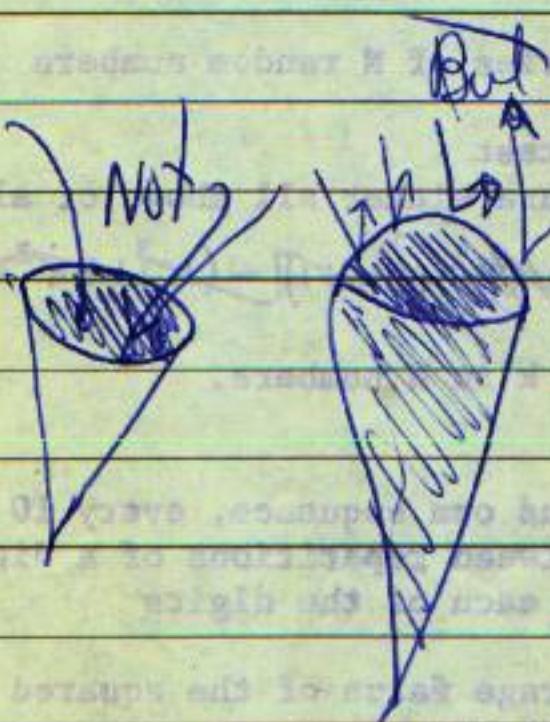
11 575C



11 575C LINKED

find Volume of cone

18



END

60 10 7

700 FORMAT Y2110H

READ Y1Y 700H JPLY JSL

~~Segment~~

- { Find from INT 1-200
- those in which bits 24 & 6
- are off but #5 is on
- & Fat
- Switch on/off states of  $5 \frac{1}{6}$
- & INT (New)
- Copy 4 low-order bits of ~~original #~~